

BASICS

`[a:s:b]` — Vector from `a` to `b` in steps of length `s`.
`linspace(a,b,n)` — Vector of `n` even-spaced numbers between `a` and `b`.
`pi`, `exp(1)` — Values of π and e (3.14159... and 2.71828...).
`clear`, `clear(x)` — Clear the values of all variables or only of `x`.
`whos`, `who` — Describe or list the defined variables.

ARITHMETIC AND LOGIC OPERATORS

`+` `-` `*` `/` — Basic operations with numbers and matrices.
`^` — Raise to a power a matrix: $a^b = a^b$.
`.*` `./` `.^` — Multiply, divide and raise to a power *elementwise*.
`&` `|` `~` — Logical operators **and** (`&`), **or** (`|`), **not** (`~`).
`all`, `any` — Test whether *all* (`all`) or *any of* (`any`) the elements of a vector satisfy a condition: `any(x>0)` Is any of the elements of `x` greater than 0?

MATRICES AND VECTORS

`[a:s:b]` — Vector from `a` to `b` in steps of length `s`.
`linspace(a,b,n)` — Vector of `n` even-spaced numbers between `a` and `b`.
`length(v)` — Length of vector `v`.
`size(M)` — Size (`rows` \times `columns`) of `M`.
`zeros(n,m)` — Matrix full of 0s with `n` rows and `m` columns. If `m` is missing, square matrix `n` \times `n`.
`ones(n,m)` — Matrix full of 1s with `n` rows and `m` columns.
`eye(n)` — Identity matrix of size `n`.
`eye(n,m)` — An `n` \times `m` matrix such that the leftmost `n` \times `n` submatrix is the identity and the rest is full of 0.
`diag(v)` — Square matrix whose diagonal is the vector `v`.
`diag(v,n)` — Square matrix whose `n`-diagonal is the vector `v`. The 0-diagonal is the principal. If `n`<0, count downwards, if `n`>0, count up.
`rand(n,m)` — Random matrix of size `n` \times `m`. The values are evenly distributed between 0 and 1.

ACCESSING ELEMENTS

If `x` is a vector

`x(i)` — Element `i`-th of `x`.
`x(i:j)` — Elements from the `i`-th to the `j`-th of vector `x`.
`x(i:end)` — Elements from the `i`-th to the last one of vector `x`.
`x(:)` — All the elements of `x`.

If `A` is a matrix

`A(i,j)` — Element `i,j` of `A`.
`A(a:b,c:d)` — Elements in rows from `a` to `b` which are in columns from `c` to `d` (i.e. a *submatrix*).
`diag(A)` — Elements in the principal diagonal of `A`.

FUNCTIONS AND UTILITIES

`sqrt` — Square root. `sqrt(x)`: square root of each element of `x`.
`sin`, `cos`, `tan` — Sine, cosine and tangent. For example, `sin(x)`, sine of each element of `x`.
`asin`, `acos`, `atan` — Inverse functions of the previous ones.
`exp` — Exponential. `exp(x)`: exponential of *each element* of `x`.
`log`, `log10` — Natural logarithm (base e) and decimal (base 10). `log(x)`: natural logarithm of each element of `x`.

FUNCTION DEFINITION

`f = @(x) sin(x) - exp(x) .* x.^2` — Defines the one-variable function `f` whose value is $\sin(x) - e^x x^2$ (always use `.*`, `./` `y .^`).
`f = @(x,y,z) x .* y - z.^2 .* y ./ x` — Defines the three-variable function `t` whose value is $xy - z^2 y/x$. (always use `.*`, `./` `y .^`).
`function [z] = patata(a, b, c) end` — Inside file `patata.m`, definition of the function `patata` which returns *one* value `z` and requires 3 parameters (`a`, `b` and `c`).
`function [Sol N M] = pototo(a, b, c) end` — Inside file `pototo.m`, definition of the function `pototo` which returns *three* values (`Sol`, `N` and `M`) and requires three parameters (`a`, `b` and `c`).

PLOTTING

`clf` — Clears the graphical window.
`hold on/hold off` — Allows (`hold on`) or prevents (`hold off`) plotting on the same graph.
`plot(y)` — If `y` is a vector, plot the sequence of values of `y`.
`plot(x,y)` — If `x` and `y` are vectors *of the same length*, plot the graph of `x` against `y` given by those values.
`plot(x,f(x))` — If `x` is a vector and `f` a function, plot the points (`x`,`f(x)`).
`fplot(f,[x0 x1 y0 y1])` — If `f` is a function, plot `f` on the rectangle `[x0, x1]` \times `[y0, y1]`.
`axis([x0 x1 y0 y1])` — Replot a graph on the rectangle `[x0, x1]` \times `[y0, y1]`.
`xlim([x0 x1]), ylim([y0 y1])` — Replot a graph with `x` varying between `x0` and `x1` (or with `y` between `y0` and `y1`).

PROGRAMMING

return — Return *immediately* from a function.

```
if(COND)
    ...
end
```

— If COND holds, perform the instructions . . .

```
if(COND)
    ...1
else
    ...2
end
```

— If COND holds, do . . .1; if it does not, do . . .2.

```
for k = a:s:b
    ...
end
```

— Loop from a to b in steps of s, in the variable k.

```
for k = v
    ...
end
```

— If v is a vector, loop in the variable k traversing the elements of v.

```
while(COND)
    ...
end
```

— Repeat the instructions in . . . while COND holds.

Assuming `nombreF.m` is a `.m` file

```
function [x1 x2] = nombreF(a,b,c)
    ...
end
```

Defines function `nombreF`, which — as, as input parameters, a, b y c and returns values x1 y x2.

ADVANCED MATRIX OPERATIONS

hilb(n) — Hilbert matrix of order n. Each entry (i, j) values $1/(i + j)$.

rref(M) — *Reduced echelon* matrix associated to M.

cond(M) — Condition number of M.

inv(M) — Inverse matrix of a square matrix (if it exists).

**** — Solution of a linear system: $A \setminus b$ solves the system $Ax = b$.

[A B] = lu(M) — LU factorization of M: On one hand, $AB = M$ and on the other, A is lower triangular and B is upper triangular.

chol(A) — Cholesky factorization of A (for A symmetric and positive definite). A matrix R such that $R^*R=A$.

POLYNOMIAL OPERATIONS

Assuming v is a vector $v=[v_1, \dots, v_n]$.

polyval(v,x) — Value of the polynomial expression $v_1x^{n-1} + \dots + v_{n-1}x + v_n$ (the degree *decreases*).

roots(v) — Roots of the polynomial $v_1x^{n-1} + \dots + v_{n-1}x + v_n$.

polyderiv(v) — Derivative (as a vector expression) of the polynomial $v_1x^{n-1} + \dots + v_{n-1}x + v_n$, that is, $[v_1/(n-1), \dots, v_{n-2}/2, v_{n-1}]$.

NUMERICAL OPERATIONS

Assuming v is a vector $v=[v_1, \dots, v_n]$.

sum(v), prod(v) — Sum and product of the elements of v.

max(v), min(v) — Maximum and minimum of the elements of v.

mean(v), var(v) — Mean and variance of the elements of v.

diff(v) — Successive differences of v. That is, $[v_2 - v_1, v_3 - v_2, \dots, v_n - v_{n-1}]$. One has that $\text{length}(\text{diff}(v))=\text{length}(v)-1$.

diff(v,k) — Successive *k-differences* of v. One has $\text{length}(\text{diff}(v,k))=\text{length}(v)-k$.

INTERPOLATION

interp1(x,y) — Given x and y two equally-sized vectors of length n, returns the interpolation polynomial (Lagrange) for the points (x, y) . It is returned as a vector $[v_1, \dots, v_n]$ (interpreted as a polynomial of degree $n - 1$).

polyfit(x,y,n) — Polynomial (as a vector) of degree n which minimizes the quadratic error with respect to the cloud of points given by x and y (equally-sized vectors).

spline(x,y) — Cubic spline interpolation function for the points (x, y) given by x and y (equally-sized vectors). It returns a *piecewise polynomial* which can be evaluated using `ppval`.